

where  $\gamma_n^2$  are the squared wavenumbers of the background waveguide modes (for lossless waveguides,  $\gamma_n^2$  are real quantities, positive or negative). Similar to nonuniform free space waves, nonuniform waveguide modes propagate along a given direction and attenuate/grow along the orthogonal one. The complex wavevector  $\mathbf{k}_n$  can be written as the sum of a real part and an imaginary part

$$\mathbf{k}_n = \beta_n \hat{\mathbf{u}}_n - j\alpha_n \hat{\mathbf{v}}_n, \quad (3)$$

where  $\beta_n$  is the phase constant of the nonuniform waveguide mode, and  $\alpha_n$  is its attenuation constant ( $\beta_n$  and  $\alpha_n$  are real numbers). From (2) and (3), we find that

$$\beta_n^2 - \alpha_n^2 = \gamma_n^2 \quad (4)$$

and

$$\hat{\mathbf{u}}_n \cdot \hat{\mathbf{v}}_n = 0. \quad (5)$$

The leaky wave in the line will excite nonuniform waveguide modes contributing to the far radiation field. The *phase* as well as *attenuation match conditions* must be satisfied by all the nonuniform modes

$$\text{Re}(k_l) = \beta_n \cos \theta_n, \quad (6)$$

$$\text{Im}(k_l) = -\alpha_n \sin \theta_n, \quad (7)$$

where  $\theta_n$  is the angle between the direction of propagation of the transmission line and the leakage direction,  $\hat{\mathbf{u}}_n$ . For *physical* waves,  $\theta_n$  must be a real number and the basic *phase match constraint* can be written as

$$\text{Re}(k_l) < \beta_n. \quad (8)$$

When  $\beta_n \simeq \gamma_n$  (i.e. when the  $n$ -th waveguide mode is almost uniform), which implies (from (4) and (6))  $\alpha_n \simeq 0$  and  $\text{Im}(k_l) \simeq 0$ , (6) can be approximated as:

$$\text{Re}(k_l) \simeq \gamma_n \cos \theta_n, \quad (9)$$

or

$$\text{Re}(k_l) < \gamma_n, \quad (10)$$

which is the approximate phase-match condition as given by (42) of [1]. When  $\beta_n$  is different from  $\gamma_n$  (or, when the excited background wave is nonuniform), though in many reported cases the condition (10) is known to apply, it does not *necessarily* follow from (8). The leaky waves with the phase constant,  $\text{Re}(k_l)$ , greater than the wavenumber,  $\gamma_n$ , recently reported in [4] and elsewhere as nonconventional leakage, are such situations.

If the condition (10) does not apply for general cases, another rigorous criterion of excitation of leakage must be searched for. It may be noted that the basic condition (8) is not useful, because unlike the wavenumber,  $\gamma_n$ , the phase constant,  $\beta_n$ , is not an independent physical parameter and is a function of both  $\gamma_n$  and  $k_l$ . In fact, as it can be shown, for a given complex propagation constant,  $k_l$ , and wavenumber,  $\gamma_n$ , there are always two sets of solutions for

$\beta_n$ ,  $\alpha_n$  and  $\theta_n$  satisfying (4), (6), and (7), one of which always satisfies the condition (8), making the criterion (8) indeterministic. Further investigation for a proper criterion of leakage valid in general situations is warranted.

## REFERENCES

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## Corrections to "TE-Mode Scattering from Two Junctions in H-Plane Waveguide"

Hyo Joon Eom

In the above paper,<sup>1</sup> there are serious printing errors that need to be corrected. The corrections are as follows: In (9) and (14),  $j$  should be replaced by  $i$ . In (35), 'when  $d = a$  and  $\alpha = 0$ ' should be replaced by 'when  $b_m = a_n$  and  $\alpha = 0$ '.

In (31), (32), (44), and (45),  $ds$  should be replaced by  $d\zeta$ . In (40) and (49)  $|s| = \sqrt{k_l^2 - (e\pi/b)^2}$  should be replaced by  $|\zeta| = \sqrt{k_l^2 - (l\pi/b)^2}$ . Equation (36) should read

$$B_m = -\pi[|d - a|e^{i\zeta|d-a|} - (-1)^m|d + a|e^{i\zeta|d+a|}]$$

. Equation (39) should read

$$r_{nm} = \sum_{l=1}^{\infty} 2 \cos(l\pi) T_{\xi\xi} [1 - (-1)^m e^{i2\sqrt{k_l^2 - (l\pi/b)^2}a}]$$

. Equation (48) should read

$$z_{nm} = \sum_{l=1}^{\infty} 2 \cos(l\pi) T_{\eta\eta} [1 - (-1)^m e^{i2\sqrt{k_l^2 - (l\pi/b)^2}d}]$$

In (56),  $e^{-ik_{zs}d}$  should be replaced by  $e^{-ik_{zs}d}$ .

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The author is with the Department of Electrical Engineering, Korea Advanced Institute of Science and Technology, Taejeon 305-701 Korea.

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<sup>1</sup>J. W. Lee and H. J. Eom, "TE-mode scattering from two junctions in H-plane waveguide," *IEEE Trans. Microwave Theory Tech.*, vol. 42, no. 4, pp. 601–606, Apr. 1994.